

LSC Use Only Number: Submission Date: Action-Date:

UWUCC USE Only Number: 91-35h

Submission Date: Action-Date:

app. 2/16/97

CURRICU University-Wide I. CONTACT	JLUM PROPOSAL COVER SHEET Senate app. 2/3 e Undergraduate Curriculum Committee
Contact Person Gerald B	uriok Phone 2608
Department Mathematics	
II. PROPOSAL TYPE (Check All Appropriate Lines)	
XCOURSE	MA 421 Advanced Calculus I
New Course*	Suggested 20 character title
X_ Course Revision	Course Number and Ful Title  MA 421 Advanced Calculus I
	Course Number and Full Title
Liberal Studies Appl for new or existing	Course Number and Fest Title
Course Deletion	• •
333,33 23,61,61	Course Number and Full Title
Number and/or Title	Change
e e	Old Number and/or Full Cld Title
	New Number and/or Full New Title
Course or Catalog Description Change	
	Course Number and Ful Title
PROGRAM:	Major Minor Track
New Program *	
	Program Name
· Program Revision* _	Program Name
Program Deletion * _	
Title Change	Program Name
	Old Program Name
III. Approvals (signatures and date	New Program Name
Department Corriculum Committee  College Curriculum Committee	14/97 Suite Bunk 9/14/97 Department Chair Department Chair College Jean D. Zell 10/15/97
Comede Carriculum Complixee	( College Dean

### Part II. Description of Curriculum Change.

- 1. New syllabus of record attached.
- 2. A summary of the proposed revision:

The current prerequisite for MA421 Advanced Calculus I is "MA 124 or 227, MA 271 with a C or better grade." The proposed revision would change the prerequisite to "MA 124, and MA 272 with a C or better grade."

#### 3. Justification/rationale for the revision:

The Mathematics Department is proposing a change in the core for all four undergraduate programs offered by the department, namely Mathematics, Applied Mathematics, Secondary Mathematics Education, and Economics/Mathematics. One aspect of this change is to extend MA271 Algebraic Structures to a two semester sequence, MA271 and MA272. MA271 will be renamed MA271 Introduction to Mathematical Proofs I, while the second course will be titled MA272 Introduction to Mathematical Proofs II. The prerequisite of MA421 will be changed to "C or higher in MA272." Faculty of the Mathematics Department have determined that the background in mathematical proofs that students acquire in MA271 is inadequate for upper level mathematics courses. Extending MA271 to a two semester sequence will provide an opportunity for students to gain a stronger background before being exposed to upper level theory oriented mathematics courses where there is an emphasis on proofs. The prerequisite change for MA421 will ensure students have the background necessary for succeeding in this course.

A second aspect of the change in the core for all mathematics programs is to replace the MA127/128/227 calculus requirement with MA 123/124. MA 127/128/227 will be eliminated as courses offered by the department. Whereas a student is now prepared for MA 421 after completing either calculus sequence, eventually only MA 123/124 will be offered. Hence MA 227 is being deleted as a prerequisite.

- 4. Old syllabus of record attached.
- 5. Liberal Studies course approval form and checklist.

Not applicable.

Part III. Letters of Support.

No other department is affected by this change.

## I. Catalog Description

MA421/521 Advanced Calculus I

3 credits
3 lecture hours
(3c-0l-3sh)

Prerequisites:

MA124 and MA 272 with a C or better grade.

Study of set theory, real number system. functions. topology of Cartesian space, sequences. convergence and uniform convergence. continuity, and uniform continuity.

## II. Course Objectives:

- 1. Students will review the basics of set theory and the real line and typical proofs on those topics.
- 2. Students will study and be expected to give examples and prove results related to the topology of the real line and sequences.
- 3. Students will develop the ability to prove results about continuity, uniform continuity, and differentiability.
- 4. (If time permits) Students will be expected to understand and prove results related to series, convergence and uniform convergence.

#### III. Course Outline/Time Schedule:

A. The Real Number System

(4 weeks)

- 1. Review of Set Theory
- 2. Constructing the Real Numbers
- 3. The Topology of the Real Line
- 4. Compact Subsets of the Real Line
- B. Functions, Sequences, Limits, Continuity

(4 weeks)

- 1. Functions and Sequences
- 2. Definition of Limits
- 3. Limit Theorems and their Proofs
- 4. Continuity
- 5. Uniform Continuity

C. Differentiation

(4 weeks)

- 1. The derivative of functions from R to R
- 2. Elementary rules of derivatives and their proofs
- 3. The Mean Value Theorem and its Consequences
- 4. The general derivative of functions from R<sup>n</sup> to R<sup>m</sup>

#### D. Series and Convergence

(2 weeks)

- 1. Infinite Series
- 2. Tests for Conditional and Absolute Convergence
- 3. Series and Sequences of Functions
- 4. Uniform Convergence

### IV. Evaluation Methods

There is variation in the weights given to evaluation methods used, but typically 40% of the grade will be determined by hand-in assignments emphasizing the writing of proofs, and about 20% of the grade will be determined by a comprehensive final examination. Approximately 5% of the grade will be determined by class activity and participation. About 35% of the grade will be determined by a mixture of quizzes, minitests, and tests. This varies with the individual instructor. One instructor typically uses 6 minitests when the course meets only two times a week. Another instructor typically uses three tests and no quizzes.

The final course grade will be determined by the total number of points accumulated on assignments and examinations, with the grading scale approximately as follows: 90% and above A, 80-89% B, 70-79% C, 60-69% D, and below 60% F.

V. Appropriate Textbooks: These books contain the appropriate material at the appropriate level and each has been used as the required textbook for the course.

Belding, David F. and Kevin J. Mitchell, Foundations of Analysis, Englewood Cliffs, NJ: Prentice-Hall, 1991
Buck, R. Creighton, Advanced Calculus, New York: McGraw-Hill, 1978.
Gaughan, Edward D., Introduction to Analysis, Monterey, CA: Brooks/Cole, 1987.

# VI. Special Resource Requirements: None.

# VII. Bibliography

Apostol, Tom: *Mathematical Analysis*, second edition. Reading, MA: Addison Wesley, 1974.

Bartle, Robert: The Elements of Real Analysis. New York: John Wiley, 1964.

Bressoud, David: A Radical Approach to Real Analysis. Washington, DC: Mathematical Association of America, 1994.

Parzynski, William R. and Philip W. Zipse, Introduction to Mathematical Analysis, New York: McGraw-Hill, 1982.

Mathematics Department Indiana University of Pennsylvania Indiana, PA 15705

Course Number: MA 421/521

Advanced Calculus I Course Title:

Credits: 3 semester hours

MA 124 or MA 227, and MA 271 with a grade of Prerequisites:

C or better

Textbook: Foundations of Analysis

David Belding - Kevin Mitchell

Prentice Hall

9/94 Revised:

#### Catalog Description:

Study of set theory, real number system, functions topology of Cartesian space, sequences, convergence and uniform convergence, continuity, and uniform continuity.

#### Course Outline/Time Schedule:

- The Real Number System
  - Irrational Numbers
  - Constructing the Real Numbers
  - The Axiom System for the Real Numbers
  - The Heine-Borel Theorem
- Functions, Limits, Continuity
  - A. Functions
  - В. Limits
  - C. Limit Theory
  - D. Other Types of Limits
  - E. Continuity
  - F. Continuity on Closed Intervals
- III. Differentiation and Integration
  - The Derivative
  - Elementary Laws of Differentiation
  - C. The Mean Value Theorem and Its Consequences

  - D. IntegrationE. Properties of the IntegralF. The Fundamental Theorems of Calculus
  - Taylor Polynomials

- IV. Sequences and Series
  A. Infinite Sequences
  B. Monotone and Cauchy Sequences
  C. Infinite Series and Convergence Tests
  D. Absolute and Conditional Convergence